4.5 Data Sources (continued)

Figure 4-3. Price and Quantity Indexes for Capital Input

	ltem	Monthly Report	Years	Page or Schedule	Line	Col.
1.	Plant Investment (A06Y-A31Y & L06Y-L31Y)	QR2A	71-82	1 & 2	-	A
2.	Telephone Price Index (A115Y-A335Y)	Bell Sys	stem Teleph	one Plant Inc	texes (T	P1)*
3.	Constant Dollar Stock-Benchmark (E114Q-E334Q & F114Q-F334Q)	Christe	nsen, Christ	ensen & Scho	ech - 19	81*
4.	Cost of Capital (A528Q)	9.5 percent 10.5 percent 12.0 percent 14.5 percent 15.25 percent	t - 1Q & 2Q nt - 3Q & 4 nt - '75 thro nt - 2Q of '6 ent - 2Q of	Embedded () of '72 thro ough 1Q of '8 80 through 10 through 10 through 10 through 10 through 40 through 40	ugh '74 0 Q of '81 IQ of '8:	•
5.	Taxes (A411Y, A413Y, A414Y, A416Y, & A418Y)	Ве	ell System S	itatistical Ma	nua]*	
6.	Revenues - Local Interstate (A701M & L701M)	MR4	72-74 75 76 77 & 78 79 80-83	1 1 1 1 2 3	26 30 32 34 21	A A A A

4.5 Data Sources (continued)

Figure 4-3. Price and Quantity Indexes for Capital Input (continued)

	Item	Monthly Report	Years	Page or Schedule	Line	Col.
7.	Revenues -					
	Local Intrastate	MR4	72-74	1	27	Α
	(A702M & L702M)		75	1	31	Α
			76	1	33	A
			77 & 78	1	35	Α
			79	2	22	Α
			80-83	3	11	A
8.	Revenues -					
	MTS Interstate	MR4	72-78	2	5	Α
	(A703M & L703M)		79	2	28	Α
			80-83	3	25	A
9.	Revenues -					
	MTS Intrastate	MR4	72-78	2	6	A
	(A704M & L704M)		79	2	29	Α
			80-83	3	37	A
10.	Revenues -					
	WATS Interstate	MR4	72-78	2	11	Α
	(A705M & L705M)		79	2	34	Α
			80-83	4	6	Α
11.	Revenues -					
	WATS Intrastate	MR4	72-78	2	12	Α
	(A706M & L706M)		79	2	35	Α
	••••••		80-83	4	14	Α
12.	Revenues -					
	PL Interstate	MR4	72-74	2	34	Α
	(A707M & L707M)		75-78	2	36	Α
			79	3	23	Α
			80,81,83	4	30	Α
			82	4	31	A

4.5 Data Sources (continued)

Figure 4-3. Price and Quantity Indexes for Capital Input (continued)

	ltem_	Monthly Report	Years	Page or Schedule	Line	Col.
13.	Revenues -					
	PL Intrastate	MR4	72-74	2	35	
	(A708M & L708M)		75-78	2	37	A
			79	3	24	Â
			80 & 81	5	14	Â
			82 & 83	5	15	Â
14.	Revenues -					
	Other Toll Interstate	MR4	72-78	Data No	t Availa	ble
	(A709M & L709M)		79	3	30	A
			80 & 81	5	22	Ä
			82 & 83	5	23	A
15.	Revenues -					
	Other Toll Intrastate	MR4	72-74	2	37	A
	(A710M & L710M)		75	2	39	A
			76-78	2	41	A
			79	3	31	A
			80 & 81	5	32	A
			82 & 83	5	33	A
16.	Revenues -					
	Misc. Intrastate (A711M & L711M)	MR4	72-75	3	6	A
	(A/IIM & L/IIM)		76-78	3	7	A
			79	4	17	A
			80 & 81 82	6	16	À
			83	6 6	15	Ā
			0.3	0	16	A
17.	Revenues - Total Interstate	MR4	** **	_		
	(A712M & L712M)	MK4	72-75 76-78	3	7	A
	······································		76-78 79	3 4	. 8	Ā
			80	6	18	Ā
			81 & 83	6	20 17	A
	•		82	6	16	A
				v	.0	A

4.5 Data Sources (continued)

Figure 4-3. Price and Quantity Indexes for Capital Input (continued)

	Item	Monthly Report	Years	Page or Schedule	Line	Col.
18.	Revenues -					
	Total Intrastate	MR4	72-75	3	8	Α
	(A713M & L713M)		76-78	3	9	Α
			79	4	19	A
			80	6	21	Α
			81 & 83	6	18	A
			82	6	17	Α
19.	Price Indexes (A721M, A723M - A727M, & A731M)	Price Inde	tes for Selec	cted Telepho	ne Serv	ices*
Net	work Varjable - Main	and Equiv. N	Main Telep	hones		
1.	In Service at End of Year (B905Y)	MR7	72-83	2	38	07
2.	Net Gain Monthly (B903M)	MR7	72-83	2	19	04

4.5 Data Sources (continued)

Figure 4-4. Data Used in Regression Analysis

BOC RAW MATERIALS INPUT

DOC RAW MATERIALS EN OT					
	Cost	Price	Quantity		
1072	528.4126	.987000	535.3726		
2072	539.9160	.994000	543.1750		
3072	491.6489	1.003000	490.1782		
4Q72	546.8987	1.016000	538,2864		
1073	579.1868	1.031000	561.7717		
2073	607.9526	1.049000	579.5544		
3Q73	640.8398	1.069000	599.4761		
4073	620.4929	1.088000	570.3059		
1074	643.0303	1.115000	576.7090		
2074	692.4280	1.140000	607,3928		
3Q74	645.1045	1.173000	549.9609		
4074	615.8218	1.208000	509.7861		
1075	697.9553	1.231000	566.9824		
2075	766.0432	1.249000	613.3252		
3075	689.1270	1,274000	540.9160		
4075	716.7209	1.297000	552.5991		
1076	809.4497	1.310000	617.9004		
2076	885.6140	1.325000	668.3882		
3Q76	787.8403	1.342000	587.0642		
4076	888.3057	1.365000	650.7734		
1077	980.0745	1.368000	716.428 7		
2Q77	1024.899	1.390100	737.2847		
3Q77	1023.220	1.410300	725.5337		
4077	901.8958	1.432400	629.6396		
1Q78	1040.848	1.451200	717.2329		
2Q78	1245.360	1.488900	836.4299		
3Q78	1046.979	1.520200	688.7119		
4Q78	1266.286	1.553800	814.9607		
1Q79	1166.220	1.586000	735.3213		
2Q79	1435.940	1.618500	887.2043		
3Q79	1322.671	1.651200	801.0361		
4Q79	1351.127	1.680500	804.0032		
1080	1474.560	1.719400	857.6013		
2080	1606.406	1.764600	910.3516		
3Q80	1558.196	1.802400	864.5120		
4080	1461.047	1.851300	789.2007		
1081	1650.115	1.900100	868.4358		
2081	1996.177	1.930300	1034.128		
3Q81	1803.223	1.977000	912.1006		

4.5 Data Sources (continued)

Figure 4-4. Data Used in Regression Analysis (continued)

BOC RAW MATERIALS INPUT (continued)

	Cost	Price	Quantity
4Q81	1808.613	2.016900	896.7292
1Q82	1801.941	2.039800	883.3911
2Q82	2085.605	2.067700	1008.659
3Q82	1975.173	2.085300	947.1887
4Q82	2171.331	2.102700	1032.639

BOC LABOR INPUT

3Q72 1924.220 .614171 4Q72 1941.337 .630146 3080.771 1Q73 1931.820 .646122 2989.870 2Q73 1972.704 .662097 2979.479 3Q73 2054.813 .678549 3028.244 4Q73 2222.905 .695478 3196.22 1Q74 2163.340 .712407 3036.66 2Q74 2207.967 .729336 3027.36 3Q74 2370.774 .750419 3159.26 4Q74 2522.429 .775657 3251.99 1Q75 2471.091 .800895 3085.41 1Q75 2471.091 .800895 3085.91 3Q75 2720.461 .851963 3193.16 4Q75 2781.950 .878388 3167.11 1Q76 2778.135 .904812 3070.40 4Q76 2776.887 .931236 2981.93 3Q76 3017.658 .951392 3171.83 3Q76 3017.658 .951392	-
2Q72 1810.603 598196 3028.731 3Q72 1924.220 614171 3133.035 4Q72 1941.337 630146 3080.771 4Q72 1941.337 630146 3080.771 1Q73 1972.704 662097 2979.479 2Q73 1972.704 662097 3028.244 3Q73 2222.905 695478 3196.227 4Q74 2207.967 729336 3027.367 2Q74 2207.967 729336 3027.367 2Q74 2370.774 750419 3159.267 3Q74 2370.774 750419 3159.267 3Q74 2522.429 775657 3251.999 4Q74 2522.429 800895 3085.41 1Q75 2471.091 800895 3085.41 2Q75 2500.829 826133 3027.15 2Q75 2781.950 878388 3167.11 1Q76 2778.135 904812 3070.40 1Q76 2778.135 904812 3070.40 1Q76 2776.887 931236 2981.93 2Q76 3017.658 951392 3171.83 3Q76 3017.658 951392 3171.83 3Q76 3017.658 951392 3171.83 1Q77 3011.135 979168 3075.12 2Q77 3066.781 993056 3088.22	
3Q72 1924.220 614171 313.3036 4Q72 1941.337 630146 3080.771 1Q73 1931.820 646122 2989.870 2Q73 1972.704 .662097 2979.475 3Q73 2054.813 .678549 3196.227 4Q73 2222.905 .695478 3196.227 1Q74 2163.340 .712407 3036.66 1Q74 2207.967 .729336 3027.36 3Q74 2370.774 .750419 3159.26 4Q74 2522.429 .775657 3251.99 4Q74 2522.429 .775657 308.541 1Q75 2471.091 800895 308.541 4Q75 2508.829 826133 3027.15 3Q75 2720.461 851963 3193.16 4Q75 2781.950 878388 3167.11 4Q76 2776.887 .931236 2981.93 2Q76 2776.887 .931236 2981.93 3Q76 3017.658	
4Q72 1941.337 630146 3080.771 1Q73 1931.820 646122 2989.870 2Q73 1972.704 .662097 2979.479 3Q73 2054.813 .678549 3028.244 4Q73 2222.905 .695478 3196.225 1Q74 2163.340 .712407 3036.666 2Q74 2207.967 .729336 3027.36 3Q74 2370.774 .750419 3159.26 4Q74 2522.429 .775657 3251.99 4Q75 2471.091 .800895 3085.41 1Q75 2471.091 .800895 3085.41 4Q75 2781.950 .878388 3167.11 4Q75 2781.950 .878388 3167.14 4Q76 2776.887 .931236 2981.93 2Q76 2776.887 .931236 2981.93 3Q76 3017.658 .951392 3171.83 3Q76 3017.658 .951392 3171.83 4Q76 3062.147	
1Q73 1931.820 6.46122 2989.6.02 2Q73 1972.704 .662097 2979.479 3Q73 2054.813 .678549 3028.244 4Q73 2122.905 .695478 3196.222 1Q74 2163.340 .712407 3036.66 2Q74 2207.967 .729336 3027.36 3Q74 2370.774 .750419 3159.26 4Q74 2522.429 .775657 3251.99 1Q75 2471.091 .800895 3027.15 2Q75 2500.829 .826133 3027.15 3Q75 2720.461 .851963 3193.16 4Q75 2781.950 .878388 3167.11 1Q76 2776.887 .931236 2981.93 2Q76 2776.887 .951392 3171.83 3Q76 3017.658 .951392 3171.83 4Q76 3062.147 .965280 3075.15 1Q77 3011.135 .999168 3075.15 1Q77 3066.78	
2Q73 1972.704 .662097 2979.473 3Q73 2054.813 .678549 3196.227 4Q73 2222.905 .695478 3196.227 1Q74 2163.340 .712407 3036.66 2Q74 2207.967 .729336 3027.367 3Q74 2370.774 .750419 3159.267 3Q74 2522.429 .775657 3251.996 4Q74 2522.429 .775657 3251.996 1Q75 2471.091 .800895 3085.41 2Q75 2500.829 .826133 3027.15 3Q75 2720.461 .851963 3193.16 4Q75 2781.950 .878388 3167.11 1Q76 2778.135 .904812 3070.40 2Q76 2776.887 .931236 2981.93 3Q76 3017.658 .951392 3171.83 3Q76 3062.147 .965280 3172.25 4Q76 3066.781 .993056 3088.22 2Q77 3066.	
3Q73 2054.813 678549 3026.248 4Q73 2222.905 695478 3196.22* 1Q74 2163.340 712407 3036.66* 2Q74 2207.967 729336 3027.36* 3Q74 2370.774 750419 3159.26* 4Q74 2522.429 775657 3251.99* 4Q75 2471.091 800895 3085.41* 2Q75 2500.829 826133 3027.15* 3Q75 2720.461 851963 3193.16* 4Q75 2781.950 878388 3167.11* 1Q76 2778.135 .904812 3070.40* 1Q76 2776.887 .931236 2981.93* 3Q76 3017.658 .951392 3171.83* 3Q76 3062.147 .965280 3172.26* 4Q76 3062.147 .965280 3075.15* 2Q77 3066.781 .993056 3088.22* 3Q77 3066.781 .993130 3189.85*	
4Q73 2222.905 .695478 3190.25 1Q74 2163.340 712407 3036.66 2Q74 2207.967 729336 3027.36 3Q74 2370.774 750419 3159.26 4Q74 2522.429 ,775657 3251.99 4Q75 2471.091 800895 3085.41 2Q75 2500.829 826133 3027.15 3Q75 2720.461 851963 3193.16 4Q75 2781.950 878388 3167.11 1Q76 2778.135 .904812 3070.40 1Q76 2776.887 .931236 2981.93 2Q76 2776.887 .951392 3171.83 3Q76 3017.658 .951392 3171.83 4Q76 3062.147 .965280 3075.12 1Q77 3011.135 .993056 3088.22 2Q77 3066.781 .993056 3088.22 3Q75 .90310 3189.87	
1Q74 2163.340 .712407 3036.363 2Q74 2207.967 .729336 3027.363 3Q74 2370.774 .750419 3159.263 4Q74 2522.429 .775657 3251.993 1Q75 2471.091 .800895 3085.41 1Q75 2500.829 .826133 3027.15 3Q75 2720.461 .851963 3193.16 4Q75 2781.950 .878388 3167.11 1Q76 2778.135 .904812 .2981.93 2Q76 2776.887 .931236 .2981.93 3Q76 3017.658 .951392 3171.83 4Q76 3062.147 .965280 3172.29 4Q76 3062.147 .991056 3088.22 2Q77 3066.781 .993056 3088.22 2Q77 3066.781 .909310 3189.87	
2Q74 2207.967 729336 3027.35 3Q74 2370.774 750419 3159.26 4Q74 2522.429 775657 3251.99 4Q75 2471.091 800895 3085.41 2Q75 2500.829 826133 3027.15 2Q75 2720.461 851963 3193.16 4Q75 2781.950 878388 3167.11 4Q75 2781.950 904812 3070.40 4Q76 2776.887 931236 2981.93 3Q76 3017.658 951392 3171.83 3Q76 3017.658 951392 3171.83 4Q76 3062.147 965280 3172.25 4Q76 3011.135 979168 3075.15 4Q77 3011.135 979168 3075.15 2Q77 3066.781 993056 3088.22	
2Q74 2270-774 750419 3159.26 3Q74 2370.774 750419 3159.26 4Q74 2522.429 775657 3251.99 1Q75 2471.091 800895 3085.41 2Q75 2500.829 826133 3027.15 3Q75 2720.461 851963 3193.16 4Q75 2781.950 878388 3167.11 1Q76 2778.135 .904812 3070.40 2Q76 2776.887 .931236 2981.93 3Q76 3017.658 .951392 3171.83 4Q76 3062.147 .965280 3172.29 4Q76 3062.147 .993056 3088.22 2Q77 3066.781 .993056 3088.22 2Q77 3066.781 .99310 3189.87	
3Q74 2512.429 .775657 3251.99 4Q74 2522.429 .800895 3085.41 1Q75 2471.091 .800895 3085.41 2Q75 2500.829 .826133 3027.15 3Q75 2720.461 .851963 3193.16 4Q75 2781.950 .878388 3167.11 1Q76 2778.135 .904812 2981.93 2Q76 2776.887 .931236 2981.93 3Q76 3017.658 .951392 3171.83 4Q76 3062.147 .965280 3172.29 4Q76 3062.147 .995056 3088.22 2Q77 3066.781 .993056 3088.22 2Q77 3066.781 .90310 3189.87	
4Q74 292.42 800895 3085.41 1Q75 2471.091 800895 3085.41 2Q75 2500.829 826133 3027.15 3Q75 2720.461 851963 3193.16 4Q75 2781.950 .878388 3167.11 4Q76 2776.887 .991236 2981.93 2Q76 2776.887 .951392 3171.83 3Q76 3017.658 .951392 3172.29 4Q76 3062.147 .965280 3172.29 1Q77 3011.135 .979168 3075.15 2Q77 3066.781 .993056 3088.22 2Q77 3066.781 .90310 3189.87	
1Q75 2471.04 826133 3027.15 2Q75 2500.829 826133 3193.16 3Q75 2720.461 851963 3193.16 4Q75 2781.950 878388 3167.11 1Q76 2778.135 .904812 3070.40 2Q76 2776.887 .931236 2981.93 3Q76 3017.658 .951392 3171.83 4Q76 3062.147 .965280 3172.29 1Q77 3011.135 .979168 3075.15 2Q77 3066.781 .993056 3088.22 1007310 3189.87 3000.00 3189.87	
2Q75 23KH.645 3193.16 3Q75 2720.461 851963 3193.16 4Q75 2781.950 878388 3167.11 1Q76 2778.135 .904812 3070.40 2Q76 2776.887 .931236 2981.93 3Q76 3017.658 .951392 3171.83 4Q76 3062.147 .965280 3172.29 1Q77 3011.135 .979168 3075.15 2Q77 3066.781 .993056 3088.22 1007310 3189.87 3189.87	
3Q75 2781.950 .878388 3167.11 4Q75 2781.950 .904812 3070.40 1Q76 2778.135 .904812 2981.93 2Q76 2776.887 .931236 2981.93 3Q76 3017.658 .951392 3171.83 4Q76 3062.147 .965280 3172.29 1Q77 3011.135 .979168 3075.15 2Q77 3066.781 .993056 3088.22 1 009310 3189.87 3189.87	6
4Q75 2781.93 1Q76 2778.135 .904812 3070.40 2Q76 2776.887 .931236 2981.93 3Q76 3017.658 .951392 3171.83 4Q76 3062.347 .965280 3172.29 1Q77 3011.135 .979168 3075.15 2Q77 3066.781 .993056 3088.22 2Q77 3066.781 .90310 3189.87	0
1Q76 2776.133 .931236 2981.93 2Q76 2776.887 .951392 3171.83 3Q76 3017.658 .951392 3172.29 4Q76 3062.147 .965280 3172.29 1Q77 3011.135 .979168 3075.15 2Q77 3066.781 .993056 3088.22 1Q77 3011.331 .9791310 3189.83	1
2076 2776.367 .951392 3171.83 3076 3017.658 .951392 3172.29 4Q76 3062.147 .965280 3172.29 1Q77 3011.135 .979168 3075.15 2Q77 3066.781 .993056 3088.22	8
3Q76 3017.638 3172.29 4Q76 3062.147 .965280 3172.29 1Q77 3011.135 .979168 3075.19 2Q77 3066.781 .993056 3088.22	5
4Q76 3062.347 3979168 3075.19 1Q77 3011.135 .979168 3078.22 2Q77 3066.781 .993056 3088.22	
1Q77 3011.135 .993056 3088.22 2Q77 3066.781 .993056 3189.87	
2077 3066.781 1009310 3189.87	
307/ 3213.373	
4077 3517.586 1.027750 2334.8	
1078 3490.049 1.040330 3318.10	
3078 3427.8//	
3Q78 3754.593 1.089518 3446.19	,,,

4.5 Data Sources (continued)

Figure 4-4. Data Used in Regression Analysis (continued)

BOC LABOR INPUT (continued)

	Cost	Price	Quantity
4Q78	3813.070	1.119595	3405.760
1Q79	4011.239	1.149670	3489.036
2Q79	3949.026	1.179746	3347.354
3079	4223.789	1.209323	3492.688
4079	4450.660	1.238400	3593.878
1080	4412.195	1.267478	3481.082
2080	4427.055	1.296556	3414.474
3080	4710.168	1.330338	3540.580
4080	4996.453	1.368823	3650.181
1081	4808.379	1.407310	3416.718
2081	5135.848	1.445795	3552.26 5
3081	5485.918	1.506456	3641.603
4081	5740.953	1.589294	3612.265
1082	6038.332	1.672132	3611.156
2082	6147.578	1.754971	3502.953
3Q82	6282.742	1.837807	3418.610
4Q82	6495.535	1.920645	3381.956

BOC CAPITAL INPUT

	Cost	Price	Quantity
1Q72	2046.480	.719819	2843.048
2072	2100.603	.730493	2875.596
3072	2364.128	.811590	2912.958
4072	2424.438	.822146	2948.914
1073	2303.562	.765510	3009.187
2073	2359.148	.773903	3048.378
3073	2427.883	.782263	3103.667
4073	2513.018	.797785	3149.994
1074	2381.146	.739707	3219.041
2074	2474.836	.759380	3259.024
3074	2570.823	.779000	3300.158

4.5 Data Sources (continued)

Figure 4-4. Data Used in Regression Analysis (continued)

BOC CAPITAL INPUT (continued)

	Cost	Price	Quantity
4Q74	2671.156	.798472	3345.333
1Q75	2818.029	.832143	3386.471
2Q75	2908.351	.851027	3417.461
3Q75	3003.406	.869863	3452.736
4Q75	3092.826	.886975	3486.939
1Q76	3200.458	.912354	3507.912
2Q76	3275.193	.927765	3530.196
3Q76	3348.016	.943155	3549.803
4Q76	3427.245	.956399	3583.491
1Q77	3578.741	.988984	3618.602
2Q77	3636.561	1,000007	3636.536
3Q77	3712.200	1.010963	3671.943
4Q77	3766.016	1.020079	3691.888
1Q78	4026.038	1.073144	3751.629
2Q78	4082.895	1.080308	3779.380
3Q78	4158.027	1.087370	3823.931
4Q78	4256.109	1.098761	3873.554
1Q79	4548.012	1.158528	3925.679
2Q79	4663.520	1.174543	3970.499
3079	4782.492	1.190529	4017.118
4079	4924.309	1.209463	4071.485
1080	5068.105	1.226436	4132.383
2080	6204.191	1.493225	4154.895
3080	6396.094	1.518648	4211.703
4080	6605.645	1.547223	4269.355
1081	6617.488	1.527365	4332.617
2081	7155.828	1.635866	4374.336
3Q81	7351.297	1.668084	4407.031
4Q81	7574.059	1.700891	4452.996
1082	7340.156	1.630826	4500.883
2Q82	8128.988	1.800749	4514.227
3082	8318.906	1.834209	4535.418
4Q82	8514.738	1.867701	4558.941

4.5 Data Sources (continued)

Figure 4-4. Data Used in Regression Analysis (continued)

BOC OUTPUT

200 001101					
	Value	Price	Quantity		
1Q72	4654.367	.819853 \	5677.074		
2Q72	4738.543	.829374	5713.395		
3Q72	4926.199	.831557	5924.066		
4Q72	5076.086	.833275	6091.727		
1Q73	5207.426	.839864	6200.320		
2Q73	5407.211	.844675	6401.531		
3Q73	5506.188	.849414	6482.332		
4Q73	5696.895	.863652	6596.281		
1Q74	5867.375	.876349	6695.254		
2Q74	6075.199	.878426	6916.008		
3Q74	6178.871	.883236	6995.719		
4Q74	6267.734	.8 90936	7035.004		
1Q75	6340.863	.905508	7002.551		
2Q75	6697.129	.925178	7238.742		
3Q75	6875.359	.937018	7337.492		
4Q75	7080.133	.951358	7442.129		
1Q76	7307.281	.971626	7520.668		
2Q76	7580.551	.987170	7679.070		
3Q76	7790. 96 5	.994356	7835.188		
4Q76	7865.410	.996897	7889.895		
1Q77	8141.727	.998660	8152.652		
2Q77	8386.500	1.000005	8386.457		
3Q77	8605.477	1.001276	8594.512		
4Q77	8873.066	1.007419	8807.727		
1Q78	9193.645	1.015010	9057.691		
2Q78	9501.496	1.017142	9341.363		
3Q78	9751.922	1.023353	9529.387		
4Q78	9930.906	1.030796	9634.215		
1Q79	10246.26	1.029173	9955.824		
2Q79	10478.34	1.026849	10204.36		
3Q79	10836.11	1.029505	10525.56		
4Q79	10965.96	1.035787	10587.09		
1Q80	11360.30	1.037848	10946.02		
2Q80	11669.23	1.047080	11144.55		
3Q80	12180.69	1.059556	11496.04		
4Q80	12442.04	1.084074	11477.11		
1Q81	12667.80	1.098570	11531.17		
2Q81	13225.96	1.110668	11908.11		
3Q81	14168.22	1.189252	11913.56		

4.5 Data Sources (continued)

Figure 4-4. Data Used in Regression Analysis (continued)

BOC OUTPUT (continued)

	Value	Price	Quantity
4Q81	14384.39	1.222916	11762.37
1Q82	14642.99	1.229872	11906.11
2082	15119.58	1.255279	12044.80
3Q82	15439.10	1.268556	12170.61
4Q82	15567.82	1.295059	12020.93

	R&D Index	Telephones	
1Q72	4.382000	59.39091	
2072	4.395000	59.86763	
3072	4.408000	60.40915	
4Q72	4.421000	61.19405	
1Q73	4.434000	61.91853	
2Q73	4.448000	62.42163	
3Q73	4.461000	62.98323	
4Q73	4.474000	63.71693	
1Q74	4.488000	64.35242	
2Q74	4.502000	64.80257	
3Q74	4.516000	65.28922	
4Q74	4.530000	65.85225	
1Q75	4.545000	66.26042	
2Q75	4.559000	66.55595	
3Q75	4.574000	67.02992	
4Q75	4.589000	67.70898	
1Q76	4.604000	68.34224	
2Q76	4.618000	68.78188	
3Q76	4.633000	69.32147	
4Q76	4.648000	70.06708	
1077	4.662000	70.72516	
2Q11	4.677000	71.21371	
3077	4.691000	71.83833	
4077	4.705000	72.72694	
1Q78	4.719000	73.56938	
2078	4.733000	74.22380	
3Q78	4.746000	74.96346	
4Q78	4.760000	75.89328	

4.5 Data Sources (continued)

Figure 4-4. Data Used in Regression Analysis (continued)

	R&D Index	Telephones	
1Q79	4.773000	76.74652	
2Q79	4.786000	77.37247	
3079	4.800000	78.06540	
4079	4.813000	78.92227	
1080	4.826000	79.67876	
2080	4.839000	80.18176	
3080	4.853000	80.67033	
4080	4.866000	81.38641	
1081	4.879000	82.05638	
2081	4.892000	82.50963	
3081	4.906000	83.02281	
4081	4.919000	83.60922	
1082	4.932000	83.95763	
2082	4.944000	84.08511	
3082	4.957000	84.28368	
4Q82	4.970000	84.61533	

5.0 APPLICATIONS

5.1 Marginal Cost of Interstate Access Services

As explained in previous sections, the purpose of this study was to develop an econometric cosmodel that could be used to estimate a marginal cost associated with providing interstate access services. In Section 3.0, the coefficient of elasticity for total operating expenses with respect to total output. K. was developed from the aggregate BOC model. The following analysis demonstrate how K can be used to produce a marginal cost for interstate access service:

$$K = \frac{\delta log C_T}{\delta log Q_T}$$

where C_T = total company operating expenses, and Q_T = aggregate demand.

For a specific service (interstate access), the coefficient of elasticity for total operating expenses in defined as:

$$K_s = \frac{\delta \log C_T}{\delta \log Q_s}.$$

where Qx = demand for interstate access service.

From Section 3.0,

$$K_s = K \times \frac{R_s}{R_T} .$$

where R_x and R_T are the interstate access service revenues and total service revenues, respectively.

Substituting for Ka:

$$\frac{\delta log C_T}{\delta log Q_s} = K \times \frac{R_s}{R_T}.$$
 Equation (1)

Since $\frac{\delta \log C_T}{\delta \log Q_x} = \frac{Q_x}{C_T} \times \frac{\delta C_T}{\delta Q_x}$. Equation (1) can be rewritten in terms of a marginal cost. $\frac{\delta C_T}{\delta Q_x}$.

where

$$\frac{\delta C_T}{\delta Q_i} = \frac{C_T}{Q_i} \times K \times \frac{R_i}{R_T}.$$
 Equation (2)

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Multiplying both sides of Equation (2) by $\frac{1}{P_a}$, where P_a is the price of interstate access service, will convert the demand Q_a into a revenue, R_a , since $R_a = P_a \times Q_a$.

The marginal cost in terms of a revenue quantity. $\frac{\delta C_T}{\delta R_s}$, is given by:

$$\frac{\delta C_T}{\delta R_s} = \frac{C_T}{R_s} \times K \times \frac{R_s}{R_T}$$
or
$$\frac{\delta C_T}{\delta R_s} = K \times \frac{C_T}{R_T}.$$
Equation (3)

Equation (3) indicates that the marginal cost with respect to service revenue quantity is constant across services. This property of the model is a result of the assumption that service prices are proportional to service marginal costs. Equation (3) can be used to calculate changes in total costs resulting from a given change in service demand expressed in terms of revenues.

5.2 Marginal Cost Factor for Use in Interstate Access Service Filing

It has been shown in the above analysis that a marginal cost can be developed from the econometric cost model. This marginal cost is based on costs and revenues for the aggregate of the BOCs as of 1982 (the last actual set of historical data used in this analysis). To be useful in supporting cost effect calculations in future interstate access service filings, the following factors must be considered in developing a future test year marginal cost:

- (1) Development of appropriate cost and price deflators for projecting 1982 marginal costs
- 2) Inclusion of gross receipts tax effects on marginal costs
- (3) Methods for identifying the marginal cost portion to be assigned to the interstate jurisdiction in accordance with FCC rules (Part 67).

1. Projection of 1982 Marginal Cost

The interstate access service marginal cost, MC_{82} , can be projected to future test periods by multiplying MC_{82} by a ratio of the Gross National Product (GNP) implicit price deflator to the weighted interstate telephone service price index. The GNP price deflators for 1982 and 1986 were obtained from the U.S. Bureau of Economic Affairs. Table 5-1 shows the revenue weights by interstate service for 1982. These weights are used in Table 5-2 to calculate the weighted interstate price index used in the projection of the 1982 marginal cost value.

Once the GNP deflators and the weighted interstate telephone price indexes are developed, the projected marginal cost can be calculated as follows:

$$MC_{82} = \frac{\delta C_T}{\delta R_g} = K \times \frac{C_{782}}{R_{782}}.$$

where K = coefficient of elasticity total op exp with respect to total output = .3810 [from model]

C_T = Total Operating Expense [1982] = \$32,998 million

 R_T = Total Revenues [1982] = \$60,769 million.

$$MC_{82} = $.20689$$

$$MC_{86} = MC_{82} \times \frac{(1986 \text{ GNP Deflator})}{(1982 \text{ GNP Deflator})} + \frac{(1986 \text{ IS Tel. Price Index})}{(1982 \text{ IS Tel. Price Index})}$$

$$MC_{86} = .20689 \times (1.138) + (.9307)$$

$$MC_{86} = $.2529$$

2. Marginal Cost Assigned Interstate through FCC Rules (Part 67)

The marginal cost developed in the projection above provides the change in total company operating expenses with respect to changes in interstate revenues. To develop the cost effects on the interstate jurisdiction, the total company marginal costs must be apportioned, using Part 67 rules, to the state and interstate jurisdiction. Analysis of the Part 67 rules indicates that the predominance of the subcategories of operating expenses are apportioned based on either a usage distribution between state and interstate, an investment distribution between the two jurisdictions, or on distributions developed from other subcategories of operating expenses. Virtually none of the operating expenses are directly assigned to the jurisdictions. (As a result, if for interstate demand response purposes the relative usage between state and inter-state is kept at the same level as for the base forecast condition, and the short run change in investment resulting from demand response is zero, then the marginal operating expense cost can be distributed between state and interstate in the same manner as in the base forecast.) Specifically, the appropriate interstate factor to apply to the total company marginal cost is developed by dividing the base forecast total interstate operating expense by the base forecast total company operating expense. The subcategories of operating expenses to be used in this calculation are those considered in the econometric model developed in this paper. In particular, they are:

- Maintenance Expense (MTCE)
- Traffic Expense (Traff.)
- Commercial Expense (Comm.)
- General Office Expense (Gen. Off.)
- Other Operating Expense (Other).

Using the individual prospective total company budget view and the prospective interstate budget view, the interstate operating expense factor. ISF, can be calculated as:

The marginal cost allocated interstate, ISMC₈₆, is given by:

$$ISMC_{86} = ISF \times MC_{86}$$

3. Marginal Cost Tax Effects

The total marginal costs and the interstate portion developed above do not consider any tax effects that would be introduced by changes in the company's operating expenses. These effects must be developed outside the model and added to the change in operating expenses to obtain a total cost change including taxes.

The only taxes that will affect the cost change are those taxes that are calculated on a gross revenues or gross receipts basis. Taxes based on net income, such as federal taxes, will not cause a change in the interstate costs because the change in operating expenses will be included in the revenue requirement that is used to calculate the past demand response rates. Since these new rates will be set to generate revenues that recover costs including the adjusted operating expenses, the post-demand response net income level (Revenues - Costs) will be the same as the predemand response net income level.

The adjustment to include the effects of gross revenues taxes on the marginal costs can be developed by multiplying $ISMC_{86}$ by one plus the appropriate gross revenues tax factor for each study area:

ATISMC = ISMC₈₆
$$\times$$
 (HGRT)

where ATISMC - after tax IS marginal cost

ORT - gross revenues tax factor (study area specific)

HGRT - 1 + GRT.

Table 5-1, 1982 Interstate (IS) Revenue Weights by Service

Service	Revenues	Fraction of Total		
MTS	11.120.4 (million)	.6640		
WATS	3.226.5 (million)	.1926		
Private Line	2,401.2 (million)	.1434		
Total	16,748.1 (million)	1.0000		

Table 5-2. Weighted IS Price Indexes for 1982 and 1986*

Yr_	MTS		WATS		PL		Total IS
	Price Index	Wig	Price Index	Wig	Price Index	Wig	Price Index
							$(g) = a \times b + c \times d + e \times f$
	(a)	(p)	(c)	(d)	(e)	(t)	·
1982	100.0	.6642	100.0	.1926	100.0	.1434	100.0
1986	91.3	.6642	88.2	.1926	107.7	.1434	93.07

. Telephone Price Indexes, Bureau of Labor Statistics

6.0 CONCLUSIONS AND FUTURE DIRECTIONS

This paper described an econometric study of the marginal cost of switched and special access. Ninety-five percent confidence intervals for marginal cost of both access services is (8.74.32.62) cents per dollar of revenue or (.0109..0407) cents per switched access minute. With other required adjustments, the marginal cost of a switched access minute appears to be roughly 1.5 cents. This value is considerably below the cost of switched access in LEC access tariffs: these average roughly 6 cents per minute at present. Prices in excess of marginal cost are a sign of the potential profitability of competitive entry, and one would expect entry and competitive pressure when prices are on the order of four times marginal cost.

Future econometric work should focus on relaxing some of the restrictive assumptions the current study makes. Foremost is the assumption that access in 1986 is identical to interstate services of the predivestiture BCCs in the 1970s. Once some historical data has been obtained in the post-divestiture environment, a cost function similar to equations (1) and (2) should be re-estimated. Since short time series data will not contain enough variation to estimate a flexible function very precisely, a pooled time-series cross-section approach should be considered.

The next most restrictive assumption is the single output formulation of the cost function which is restrictive in the sense that it forces the marginal cost measure for all services to be the same. 32 Such results cannot be used to assess the relative competitive positions of LEC switched and special access services without some further physical dimension of output. Unfortunately, estimation of multi-output cost functions - though straightforward theoretically - has not been successful using short time-series data. 33 Possibly, the additional variation in output obtainable from pooled time-series and cross-section data might make distinct statistical estimates of cost elasticities of different services possible.

Finally, the assumption that all predivestiture BOCs possessed the same technology and faced the same factor prices should be relaxed. To this end, individual companies can take the data and methods presented in this study and estimate a cost function from predivestiture data that is specific to one company. For use in interstate access tariff filings, this would probably be preferable to the current reliance on a national study.

^{31.} Although it is tempting to estimate directly the marginal cost of access by estimating a cost function for access, this is unlikely to be meaningful. The process which assigns costs to services (Parts 67 and 69 of the Commission's Rules) has no economic validity and it is difficult to assume that a firm would try to minimize that cost, given factor prices and levels of interstate demand.

^{32.} It is not restrictive in the sense that any multi-product monopolist will price so that the marginal cost associated with a additional dollar's revenue is one dollar for every service.

^{33.} Christensen, Christensen, and Schoech (1983), op. cu., or Nadiri and Schankerman (1981), op. cu.

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